

Name: \_\_\_\_\_

**Math Club: Contest Week Six**

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**Release Date:** April 19, 2023

**Instructions:** Solve the following problem the best you can, first to submit the correct solution via email or the secretaries in Room 332 (with time stamp) wins!

**Problem 1.** Fill out the side-length of every member in the below diagram to prove that given  $\theta_\alpha = \arctan(\alpha)$  and  $\theta_\beta = \arctan(\beta)$  respectively, it follows that

$$\theta_\alpha + \theta_\beta = \arctan(\alpha) + \arctan(\beta) = \arctan\left(\frac{\alpha + \beta}{1 - \alpha\beta}\right).$$

Some angles and sides have already been filled in for clarity,

